# Statistics performance of elementary and middle school students in the context of D-Estat 

# Desempenho em Estatística de estudantes do Ensino Fundamental, no contexto do DEstat 

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#### Abstract

We analyzed the statistical performance of 1,305 students from 1st to 9 th grade, in elementary and middle schools, in four public schools in the state of Bahia-Brazil, in the context of a collaborative university-school research (D-Estat). We built three instruments, according to the education level, from which we analyzed three issues involving qualitative, discrete and continuous variables; conversion of native language data to bar graphs; reading of frequency distribution and two-way tables; calculation of mean, median and mode. The main results show that performance falls substantially from one level to another, but within each school grade there is a growing trend, greater in Elementary School, signaling stagnation in the Middle School. The results indicate the need to elaborate teaching sequences validated in the reality of the schools, which allow the active role of students, in the learning processes and, consequently, for statistical literacy.


Keywords: Teaching of statistics; Elementary and middle school; diagnostic study; D-Estat.

## Resumo

Analisamos o desempenho em Estatística de 1.305 estudantes do $1^{\circ}$ ao $9^{\circ}$ ano, do ensino fundamental, de quatro escolas públicas do interior da Bahia, no âmbito de uma pesquisa colaborativa universidade-escola (D-Estat). Construímos três instrumentos, de acordo com o nível de ensino, dos quais analisamos três questões que envolvem variáveis qualitativas, discretas e contínuas; conversão de dados em língua materna para gráficos de barras simples; leitura em tabelas simples e de dupla entrada; cálculo da média, mediana e moda. Os principais resultados mostram que o desempenho cai substancialmente de um nível para outro, mas dentro de cada nível se observa uma tendência crescente, maior nos anos iniciais, sinalizando estagnação nos anos finais. Os resultados sinalizam que é preciso elaborar sequências de ensino validadas na realidade das escolas, que possibilitem o papel ativo dos estudantes, em seus processos de aprendizagem e, consequentemente, para o letramento estatístico.

Palavras-chave: Ensino de Estatística; Ensino Fundamental; estudo diagnóstico; D-Estat.

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## Introduction

The insertion of Statistics contents in Elementary Education, in the curricular component of Mathematics in Brazil, was made official in 1997, with the publication of the National Curriculum Parameters - PCN (MEC, 1997 and 1998), forming one of the four blocks, called "Data Handling". This trend was ratified by the National Common Curricular Base - BNCC (MEC, 2018), which included its contents in one of the five thematic units called "Probability and Statistics".

However, based on our experience as teachers in initial and continuing education training courses; developing research on teaching and learning statistics in public schools; constructing didactic materials and supervising Master's programs in Mathematics Education, we verified that school teachers do not sufficiently address these contents, and when they do they give more importance to the technical and operational aspects, with a fragmented, reproductive approach, disjointed from social themes and disconnected from the students' reality, thus the "teach for teaching" the "calculation for calculation," reproducing meaningless knowledge to the student, as pointed out by Campos, Wodewotzki and Jacobini (2013).

Therefore, with regard to this problem, we implemented the research entitled "Professional development of teachers who teach Mathematics, D-Estat" (Santana \& Cazorla, 2018), carried out in the university-school partnership, intended to form a collaborative group in order to verify the viability of a model to train in-service teachers, which can independently develop and implement teaching strategies, in particular to build and validate teaching sequences, which guarantee student learning in the school environment, while respecting school culture and times.

We chose the thematic unit of Statistics because of the demand of teachers from partner schools, who recognize the importance and fragility of their knowledge and because Statistics allows, from an interdisciplinary perspective, to specifically work on Mathematics content, with transversal themes, where the student has an active role in building his/her learning process.

We started the research by conducting a diagnostic study in order to map the domain of statistical concepts that students developed over the nine grade of schooling, in order to guide the construction of the teaching sequences. This diagnostic study will also be carried out at the end of the research to verify how much this teacher training model contributed to the students' learning process.

For the selection of the statistical contents addressed, we refer to the curricular guidelines for teaching Statistics in Elementary Education and the principles that should guide this teaching, namely: statistical literacy, the investigative cycle and some assumptions of Critical Mathematics Education, which support the D-Estat, and the reading levels of graphs proposed by Curcio (1989) and of tables proposed by Wainer (1992), which help us to analyze the tasks. Below, we present some of related works, which allow us to discuss the
results; the methodological path, the main results of the diagnostic study and, finally, some of the considerations presented.

## Curricular teaching guidelines for Statistics in Elementary Education

With regard to specific knowledge for the area of Mathematics, the PCN stipulated four content blocks: Numbers and operations, Space and Form, Greatness and Measures and Data Handling. BNCC has stipulated five thematic units: Numbers, Algebra, Geometry, Quantities and Measures, and Probability and Statistics. The statistical concepts that were presented in the Data Handling block became part of the thematic unit Probability and Statistics, as shown in Table 1.

Table 1- Statistical concepts indicated in the PCN and BNCC


Source: MEC (1997, 1998 and 2018).
The statistical concepts listed in Table 1 are practically the same in both documents, with the BNCC reinforcing the need for methodological work with research from the 1st to the 9th grade, with the planning and execution of sample research aimed at the social reality. In addition, it is expected that schools will make it possible to develop education competencies and ability for students.

We emphasize that the research group that develops D-Estat in schools believes that Statistics is a powerful tool that can contribute to the education of the general public, allowing them able to interpret the world. For that, some principles must be assumed for its teaching of statistical literacy, the investigative cycle, the perspective of Critical Mathematics Education, that is, to empower students with a form of Statistics that is useful for their personal life and in society.

## Statistical Literacy and Critical Mathematics Education

The use of statistics concepts and procedures in the reading and modeling of the phenomena that permeate the world has been called statistical literacy which, for Gal (2002),
goes beyond the domain of statistical procedures, with the general public's competence to discuss or communicate their understanding regarding information, expressing opinions on such implications and form the conclusions drawn.

This author proposes a statistical literacy model formed by two components: one cognitive and the other attitudinal. The cognitive one consists of five elements: literacy skills, statistical knowledge, mathematical knowledge, context knowledge and the ability to formulate critical questions. The attitudinal one is composed of two elements: critical stance, beliefs and attitudes.

Operationalizing elements of the Gal (2002) model in the classroom requires experiencing all the logic of statistical investigations, with a critical and reflective focus. Therefore, we agree with Cazorla and Santana (2010) when they state that "in order to provide statistical literacy to the student, we also need to develop statistical thinking, so that the student will critically reflect on all phases of the research" (p.13).

Also observed is that criticality is present in the two components of Gal's model (2002), given that the ability to elaborate critical questions concerns the population's ability to question whether that concept used is adequate or if another one could have been used, while the critical stance concerns the ability to position oneself in face of results of the investigation.

Skovsmose (2008) discusses the social role of mathematics in favor of democracy, viewing the teaching of mathematical content as a possibility for individuals to develop their critical ability within any context.

We believe that the perspective of statistical literacy, defended by Gal (2002), is in line with the perspective of Critical Mathematics Education proposed by Skovsmose (2008) that places the teaching of Mathematics beyond the teaching of contents, with a perspective of promoting in subjects a form of critical analysis of the reality in which they are inserted, contributing to the emancipation of students.

Contemporary reality is presented in different forms of representation. In the media, information is commonly displayed in tabular or graphical representation. If the intention is to contribute to broaden students' world reading, then schools fundamentally need to help them advance in their reading levels and data interpretation presented in different representations.

To analyze the level of reading of information contained in graphs, we turn to Curcio (1989) who stipulated three different understanding levels of reading graphs: "Reading the data," referring to a literal reading of the elements in graphs, without requiring the reader knows how to interpret the data beyond what is actually presented and perceptible in the representation, with a very low cognitive cost, such as finding the minimum or maximum value; "Reading between data" includes the interpretation and integration of data in the graph and requires the ability to compare quantities and the use of other mathematical concepts. This type of reading requires a certain degree of logical or pragmatic inference such as, for
example, identifying in which period there was greater growth or the variable that experienced the greatest variation; and "Reading beyond the data", which is a more complex level and asks the reader for a global interpretation, not only of the data contained in the graph, but also understanding the phenomenon or the problem which emerges from the data.

Similarly, Wainer (1992) proposed three levels of understanding for reading and interpreting tables: "Elementary level", when the reader extracts specific data from the tables, which do not require any action for their comparison and/or analysis; "Intermediate level", when the reader interpolates and identifies what are the relationships between the data that are shown in the tables; and, "Advanced level", when it involves a broader understanding of the structure of the data presented in its entirety, generally comparing trends and analyzing implicit relationships in the tables.

## Research on student performance in Statistics

Cobo and Batanero (2004) evaluated the understanding of arithmetic mean and its properties in 53 high school students, who solved four open problems and concluded that although the idea of the mean is apparently simple, the research results indicated that for students to be successful, they must mobilize various numerical ideas in problem solving, such as the distributive property of addition and multiplication, or the inversion of the mean algorithm. In addition, they must discriminate properties that although valid for addition and multiplication, cannot be generalized to find the overall mean.

Mayén, Cobo, Batanero and Balderas (2007) studied the understanding of mean, median and mode in 125 Mexican students, aged 17 and 18, and compared the results with those of Spanish students who were 15 and 16 years old and who were in the last grade of Secondary Education. Among the results, we highlight that the researchers found that when calculating the median, students forget to order the data and that they cannot find the median with an even number of data, because "they do not know how to solve the indeterminacy produced by having two central values" (p. 196).

Luna and Carvalho (2019) analyzed the performance of 100 students (from the $6^{\text {th }}$ and $9^{\text {th }}$ grades of elementary and middle schools and the $3^{\text {rd }}$ grade of high school from a private school in Pernambuco) on five questions about arithmetic mean, involving different meanings of this concept in situations with and without graphical representations. The results obtained showed that the level of education was a determining factor in performance, and was considered below expectations, highlighting the participants' difficulty in division. It was observed that graphical representation negatively influenced the students' performance and that they mistakenly conceive the arithmetic mean as being: the sum of a set of values, a number that is divided by two, the central term of a set of values arranged in increasing order (median), or a number ending in zero.

Studies show that mistakes are not limited to students. Santos and Branches (2019), for example, investigated errors in statistical graphs published in the media and found several problems, such as: the absence of the ordinate axis, scale or grid lines, graph bars with disproportionate widths and heights, incompatibility of data labels with the measurements Zetetiké, Campinas, SP, v.28, 2020, p.1-25-e020016
presented, omission of zero and scale interruption at the beginning of the vertical axis in line graphs, among other problems.

Teixeira (2016) carried out a bibliographic research on teaching and learning content of Statistics and Probability in Basic Education. The researcher states that these contents contain elements that are very attractive to students, not only because they are present in their daily lives, but also because of the potential for developing interdisciplinary activities with the understanding and appropriation of concepts specific to society, such as insertion and social participation and politics.

Using the investigative cycle, other studies also link investigations to statistical literacy. Santana (2016) investigated the perceptions of a $3^{\text {rd }}$ grade high school class at a state school in Minas Gerais that emerged after conducting investigative activities in groups of three or four students in which they chose the topic to be investigated: violence, internet, drugs, consumerism, accessibility, bullying and corruption. Such themes were developed using the phases of the investigative cycle, which according to the researcher, favored the development of characteristics of statistical literacy and student motivation, as they made the activities more pleasurable.

Nascimento, Paula and Catarino (2018), used the investigative cycle with 5th grade students in a public school in Portugal and discussed the results of a student. The approximation between reality and content allowed the learning of frequencies (absolute, relative and percentages), in addition to the registry of counts, construction of a statistical table and bar graph. The researchers concluded that the investigative activity in the context of the student's daily life enabled the use of different registries, processing and conversions, which contributed to the movement of meanings and senses.

Also with a focus on the interest of students, Carvalho, Oliveira and Monteiro (2019) proposed teacher training to 11 indigenous teachers of the early grade of elementary schooling. The teachers planned an investigation on the water resources in the villages, discussing the theme and conducting data collection through interviews with the community. The results showed that students experienced significant and critical learning, had a reasonable numerical sense to express the research results, as they estimated quantities and represented them by using circle and bar graphs. However, the researchers considered that specific conceptual aspects in the construction of graphs were still necessary to improve students' statistical literacy, in particular those related to the organization and systematization of statistical information and the use of scale in the bar graph.

It is observed in this survey, that regardless of the level of education or cultural characteristics of students, teaching practices that privilege the use of the themes chosen, or that are of their interests, addressed within the perspective of the investigative cycle, enhance the development of statistical knowledge and critical stance that can contribute to promoting social equality. These considerations will be present in the teaching sequences that will be planned and developed together with the teachers in the D-Estat project.

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## Methodological path

The research involved four schools, 65 classes and 1,305 students distributed over the nine elementary and middle school, in the interior of Bahia, distributed by school grade according to Table 2.

The instruments were designed to accompany the mastery of concepts over the nine grade and took into account the nuances of school grade, therefore we developed three instruments: one for the $1^{\text {st }}$ level (1st to 3 rd grades), another for the $2^{\text {nd }}$ level ( $4^{\text {th }}$ and $5^{\text {th }}$ grades) and another for the Middle School ( $6^{\text {th }}$ to $9^{\text {th }}$ grades).

In this work we analyze three questions, common to the instruments of these three levels.

Table 2 - Number of subjects involved in the research, by school grade

| Fundamental Education | Education levels | School grade | Expected age | No. of schools | No. of classes | No. of students |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ElementarySchool | $1^{\text {st }}$ | $1^{\text {st }}$ | 6 | 1 | 4 | 47 |
|  |  | $2^{\text {nd }}$ | 7 | 1 | 4 | 60 |
|  |  | $3^{\text {rd }}$ | 8 | 1 | 6 | 102 |
|  | $2^{\text {nd }}$ | $4^{\text {th }}$ | 9 | 1 | 3 | 59 |
|  |  | $5^{\text {th }}$ | 10 | 1 | 5 | 104 |
| Middle School | $3^{\text {rd }}$ | $6^{\text {th }}$ | 11 | 3 | 15 | 314 |
|  |  | $7^{\text {th }}$ | 12 | 3 | 12 | 248 |
|  |  | $8^{\text {th }}$ | 13 | 3 | 10 | 222 |
|  |  | $9^{\text {th }}$ | 14 | 3 | 6 | 149 |
|  |  | Total |  | 4 | 65 | 1.305 |

(*) Although this nomenclature is not officially used, we use it to facilitate understanding the work.
Source: D-Estat data.
The $1^{\text {st }}$ level instrument comprised three questions, two with discrete variables and one with nominal qualitative (Table 3). The order of magnitude of the numbers was up to 25 and involved addition and division operations, in an intuitive concept of dividing. The data were presented in the native language, requesting the conversion to the graphic register and a statistical table, requesting the determination of the sum, the maximum, the minimum, the mode, the mean. From the qualitative variable, the mode and sample size were requested.

Table 3 - Structure of the instrument for the 1st level (1st to 3rd grade)

| Question | Variable | Nature of <br> the <br> variable | Order of <br> magnitude / <br> operations | Initial | Graph | Statistics <br> (summary <br> measures) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Q1 | Number of <br> marbles | Discreet <br> (genuine) | Up to 15, <br> addition, <br> division | Native <br> language | Bar graph | Maximum, sum, <br> mode, mean |
| Q2 | Number of <br> chocolate <br> snacks | Discreet <br> (genuine) | Up to 15, <br> addition, <br> division | Table |  | Maximum, sum, <br> mode, mean |

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| Q3 | Favorite Pet | Nominal <br> qualitative | Up to 25, <br> addition | Frequency <br> distribution <br> table | Sample size <br> (sum), mode |
| :---: | :---: | :---: | :---: | :---: | :---: |

Source: D-Estat data.
The three questions of the $2^{\text {nd }}$ level instrument ( $4^{\text {th }}$ and $5^{\text {th }}$ grades) had the same wording as the $1^{\text {st }}$ level instrument, however the complexity was due to the order of magnitude of the numbers that reached 50, and because instead of asking for the extraction of the minimum and maximum, we requested the median. In addition, in Question 2 the data went from a table to two-way table, requesting the sum by lines, as shown in Table 4.

Table 4 - Structure of the instrument for the $2^{\text {nd }}$ level ( $4^{\text {th }}$ and $5^{\text {th }}$ grade)

| Question | Variable | Nature of the variable | Order of magnitude / operations | Representation |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Initial | Graph | Statistics (summary measures) |
| Q1 | Number of marbles | Discrete (genuine) | Up to 42, addition and division | Native language | Bar Graph | Sum, mode, mean, median |
| Q2 | Number of chocolate snacks per day | $\begin{aligned} & \text { Discrete } \\ & \text { (genuine) and } \\ & \text { qualitative } \end{aligned}$ | Up to 30, addition and division | Two-way table |  | Sum, mode, mean, median |
| Q3 | Favorite pet | Nominal qualitative | Up to 50, addition | Frequency distribution table |  | Sample size, mode |

Source: D-Estat data.
The three questions of the instrument for the Middle School (6 $6^{\text {th }}$ to $9^{\text {th }}$ grades) maintained the same structure as the instruments of the Elementary School ( $1^{\text {st }}$ to $\left.5^{\text {th }}\right)$, with some changes (Table 5). In Question 1, we just changed the name of the variable. In Question 2 , in addition to the data displayed in a two-way table, we requested the sum and mean of the rows and columns, a property of the mean and comparison. In Question 3 we went from statistical table to Two-way table, requesting the relative frequency and the perception of relationships between variables.

Table 5 - Instrument structure for the Middle School (6th to 9th grade students)

| Question | Variable | Nature of the variable | Order of magnitude / operations | Representation |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Initial | Graph | Statistics (summary measures) |
| Q1 | Amount spent at the bakery | Continuous (discretized) | Up to 50, addition, division, sort | List | Bar Graph | Sum, mode, mean, median |
| Q2 | Student scores in two tests | Continuous (discretized) x qualitative | Up to 50, addition, division | Two-way table |  | Sum, mean, mean property, comparison |
| Q3 | Favorite pet by gender | Two nominals | Up to 200, addition, division | Two-way table |  | Sample size, mode, relative frequency |

Source: D-Estat data.

As we can see, the last instrument is more complex than the previous ones, since we requested reading beyond the data. However, it only contemplates the skills recommended by the BNCC and, therefore, it is expected that such content will be in the students' domain. An important question was whether students knew the names of measures of center so it was asked explicitly.

All ethical procedures for research with human beings were followed, such as filling out the Free and Informed Consent Form (FICF), authorization from the school management, and others.

The instrument was answered between May and June 2018. The students were at the beginning of the school year (strike and delay of the school year) and answered the instrument individually, during class time, under the supervision of the class teacher, who was asked not to interfere with the students' responses.

The answers were categorized as correct and not correct (wrong and blank entries) and we created the variable "percentage of correct answers," and the data were transcribed to an electronic spreadsheet.

## Results and discussion

In this section we present the results in three subsections according to the levels, and in the fourth section we draw a parallel of these three levels.

Performance of $1^{\text {st }}$ level students ( $1^{\text {st }}$ grade to $3^{\text {rd }}$ grade)
Question 1 (Figure 1), presented a discrete variable, with five native language data and requested six tasks: conversion of the data to a bar graph, providing the Graph's framework (G. Bars); identify the child who had the maximum (Maximum) value; the maximum value (MaxValue); the total of marbles (Sum); identify the Mode (Mode) and calculate the mean (Mean), and the Mode and Mean were requested without mentioning this nomenclature.


Q1b. Which child has the most marbles?

Q1b1. How many?
Q1c. In all, how many marbles do the five children have?

Q1d. Among the number of marbles for each child, what is the amount that is repeated most often?
Q1e. To start the game Dara had the idea of putting all the marbles together and sharing the marbles equally among all the children. How many marbles did each child have?

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Figure 1 - Statement of Question 1 of the 1st level.
Source: D-Estat data.

In Figure 2, we can see that performance increases with schooling in all concepts, with the exception of mode and in determining the maximum. In general, $1^{\text {st }}$ grade students perform poorly. In tasks that requested reading the data, without making calculations (Maximum and Mode), the performance was above $50 \%$, and the worst performance was in the calculation of the mean, especially in the $1^{\text {st }}$ grade.


Figure 2 - Percentage of correct answers of 1st level students in Question 1, per school grade.
Source: D-Estat data.
Question 2 (Figure 3) presented a discrete variable, with four data points arranged in a statistical table and requested for six tasks: the total (SumC); identify the child who ate the least (Minimum); the minimum value (MinValue); identify the implicit Mode (Mode); identify the value of Mode (ModeValue) and divide it into equal parts (Mean).


Figure 1 - Number of chocolate snacks each grandson ate

| Grandchildren | Number of chocolate <br> snacks |
| :---: | :---: |
| Clara | 3 |
| Luiz | 4 |
| Bia | 1 |
| Nina | 4 |
| Total Chocolate snacks |  |

Q2a. How many chocolate snacks did Grandma prepare in all?
Q2b. Who ate the least amount of chocolate snacks?

Q2c. How many chocolate snacks did they eat?
Q2d. Were there grandchildren who ate the same amount of chocolate snacks?

Q2e. If so, how many chocolate snacks did they eat each?

Q2f. If Grandma had said that all grandchildren should eat the same amount of chocolate snacks, how many should each child eat?

Figure 3 - Statement of Question 2 of the 1st level.

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Source: D-Estat data.
In Figure 4, we observe that the $3^{\text {rd }}$ grade students present good performance, including those of the $1^{\text {st }}$ grade, signaling that the students have the elementary level of reading tables (Wainer, 1992) and with the fact that the data are in their native language or that the statistical table did not interfere with performance.


Figure 4 - Percentage of correct answers of 1st level students in Question 2, per school grade.
Source: D-Estat data.
Question 3 (Figure 5) presented a qualitative variable in a frequency distribution table and requested two tasks: "How many students answered the question?" (Sum) and, "What is the favorite pet that most students chose?" (Mode). The results presented in Figure 6 confirm that the participants have an elementary level of table-reading ability, because to identify the favorite pet they needed to look for the maximum value (modal frequency) and associate the category (dog). Most students were unable to even perform the addition to find how many students answered the question.

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Q3. The school teacher asked the students what their favorite pet was and she organized the data in the Figure 2:
Figure 2 - Number of students according to favorite pet

| Favorite pet | Number of <br> students |
| :---: | :---: |
| Cat | 7 |
| Bird | 2 |
| Dog | 8 |
| Turtle | 3 |
| Others (monkey, tamarin <br> monkey, etc.) | 3 |
| None | 2 |
| Total students |  |

Figure 5 - Statement of Question 3 of the 1st level.

|  |  |  |  |  | 100 |
| ---: | ---: | ---: | :---: | :---: | :---: |

Figure 6 - Percentage of correct answers of 1st level students in Question 3, per school grade.

Source: D-Estat data.
Concluding the analysis of student performance in the $1^{\text {st }}$ level, we present Figure 7. It is observed that the percentage of blank answers in each item is less than $10 \%$ and the concept of dividing in equal parts was the one that presented more blank answers (Q1f Mean) and (Q2f-Mean). This result seems reasonable considering that in the $1^{\text {st }}$ level the concept of division is one of the last to be taught and its consolidation takes longer than addition, subtraction and multiplication.


Figure 7 - Percentage distribution of correctness, error and blank, by item, of $1^{\text {st }}$ level students. Source: D-Estat data.

## Second level of students' performance (4 ${ }^{\text {th }}$ and $5^{\text {th }}$ grade students)

Question 1 had the same wording as the 1st level instrument, increasing the amount of data from 5 to 7 and the values: "Seven children are playing marbles in the schoolyard. João
has 4, Dara has 6, Caio has 4, Ivo has 10, Lucas has 9, Ana has 4 and Enzo has 5." The items requested: to convert the native language data to a bar graph (G. Bars); find the total of marbles (Sum); identify the value that is repeated most often (Mode); divide into equal parts (Mean), order (Order) and find the value that occupies the central position (Median).

In Figure 8 we can see that, in general, students did better in converting their native language data to the graphic register and find the mode; however, only half managed to add the quantities and less than a third managed to find the mean. We expected the ordering task to be relatively simple, however less than $42.3 \%$ managed to do it; similarly, we expected that finding the Median was an intuitive and easy task, since finding the central position was immediate, since the number of data was seven (odd), just reading the value of the data that occupied the 4th position; however, less than a quarter of the students were able to accomplish this task. As in the 1st level, we observed that 4th and 5th grade students have difficulties in all items that require performing any calculation.


Figure 8 - Percentage of correct answers for 2nd level students in Question 1, per school grade.
Source: D-Estat data.
Question 2 (Figure 9) was similar to that of the 1st level, however the data were in a two-way table requesting eight tasks: add the values of the lines (Sum L); add the column values (SumC); order the total number of chocolate snacks (Order); find the value that occupies the central position (Median), and three means (Mean1, Mean2, Mean3).

> Q2. Grandma Maria prepared chocolate snacks for her grandchildren over the weekend and there were none left! She counted how many chocolate snacks each grandson ate each day and registered in Figure 1:

Figure 1 - Number of chocolate snacks that each grandson ate over the weekend.

| Grandchildren child ate | Number of chocolate snacks <br> each |  |  |
| :---: | :---: | :---: | :---: |
|  | Saturday | Sunday | on the <br> weekend |

Zetetiké, Campinas, SP, v.28, 2020, p.1-25-e020016

Q2a. Fill the Figure with the total of chocolate snacks that each grandson ate over the weekend.
Q2b. Fill the Figure with the total of chocolate snacks consumed on Saturday, Sunday and the weekend.

Q2c. Place in ascending order the number of chocolate snacks consumed by the grandchildren over the weekend:

| 1st <br> position | 2nd <br> position | 3rd <br> position | 4th <br> position |
| :---: | :---: | :---: | :---: |

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| Clara | 4 | 5 |  | Q2d. What is the amount of chocolate snacks that occupies <br> the central position? |
| :--- | :--- | :--- | :--- | :--- |
| Luiz | 5 | 6 |  | Q2e. If Grandma had said that all grandchildren should eat <br> the same amount of chocolate snacks, how many chocolate <br> snacks should each eat: on Saturday? <br> Q2f. On Sunday? |
| Bia | 3 | 5 |  | 0 |
| Q2g. On the weekend? |  |  |  |  |

Figure 9 - Statement of Question 2 of the 2 nd level ( $4^{\text {th }}$ and $5^{\text {th }}$ grade students).
Source: D-Estat data.
In Figure 10, we can see that most students were able to add by line; but in the sum per column the performance dropped to less than a third. The ordination did not exceed $40 \%$; virtually no student was able to find the value of the central position, which indicates that the median for amount of data is not intuitive and needs instruction. Finding the three mean was around $25 \%$, which we consider an unsatisfactory result, since the order of magnitude of the numbers was small, as well as the amount of data.


Figure 10 - Percentage of correct answers for 2nd level students in Question 2, per school grade. Source: D-Estat data.

Question 3 was similar to that of the 1st level, with slightly higher numbers. In the case of Mode, we found that only $42.4 \%$ in the 4 th grade and $76.9 \%$ in the 5 th grade were able to identify it. As for the sum, we verified that only $18.6 \%$ of the 4 th grade and $26 \%$ of the 5 th grade were able to correctly add the six numbers, which indicates a lower performance to that of the 1st level.

Finalizing the analysis of the performance of the $2^{\text {nd }}$ level students we present Figure 11. We observed that the number of blank answers increased considerably in relation to the 1st level and the item that stood out was the one that requested the quantity of chocolate snacks consumed on Saturday, Sunday and over the weekend (Q2b-SumC), which required

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the sum of small values. We believe that, in this case, the tabular representation was an obstacle, because it presented several data points, in several columns, which is not commonly used in school.


Figure 11 - Percentage distribution of correct, error and blank answers, by item, of $2^{\text {nd }}$ level students. Source: D-Estat data.

## Performance of students in the Middle School ( $3^{\text {rd }}$ level)

Question 1 had a structure similar to that of the $2^{\text {nd }}$ level instrument, changing only the name of the variable: "What Danilo's grandfather spent at the bakery during the past week, as shown in the following list (followed by the days of the week and the expense values from Monday to Sunday: $4,4,4,5,6,10,9) "$. Nine tasks were requested: convert the list data to a bar graph (G.Bars); find the total spent (Sum); identify the value that is repeated most often (Mode); explain the name of the Mode (N_Mode); divide the total spent by seven days: "Next week, Danilo's grandfather will spend the same amount, but in equal amounts every day. How much will he spend each day? (Mean); explain the name of the mean (N_Mean), order the values (Order); find the value that occupies the central position (Median) and explain the name of the Median (N_Median).

In Figure 12, we see that the students did better in converting the data to the graphical representation and performing the sum. In determining Mode, we see a very large variation reaching only $53 \%$, the same for mean, which does not even reach $27.9 \%$. The median performance did not exceed $32.2 \%$. The results indicate performance stagnation in relation to schooling.

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Figure 12 - Percentage of correct answers for Middle Scholl students in Question 1, per school grade. Source: D-Estat data.

As for the names of measure of center, virtually no students knew the answer. We observed that the majority of students made a mistake in ordering, since the data were ordered up to the penultimate element, which may have been misleading. However, this fact did not interfere in determining the Median, since the central position remained unchanged and, for this reason, the performance was slightly better than in the ordering.

Question 2 (Figure 13) was similar to that of the 2nd level, with the difference that in addition to the sum of the lines, the calculation of the mean, the lines and the columns were explicitly requested. The nine tasks were: sum and mean per lines (MeanL); sum by columns (SumC); mean in the 1st test (Mean1); mean in the 2nd test (Mean2); the mean in the two tests (Mean3); compare student means with the established limit and make a decision (Comparison1)"; mean property (Mean Prop); quantify the impact on the mean (How much), and finally, again comparison and decision making (Comparison2).

Q2. The math scores of a group of five students are the following.

Figure 1 - Score of five students in both tests

| Student | $1^{\text {st }}$ <br> test | $2^{\text {nd }}$ <br> test | Total in <br> both <br> tests | Average <br> of both <br> tests |
| :--- | :---: | :---: | :---: | :---: |
| Bia | 7 | 3 |  |  |
| Luiz | 7 | 3 |  |  |
| Cléo | 8 | 4 |  |  |
| Nina | 6 | 2 |  |  |
| João | 7 | 3 |  |  |
| Total group <br> scores |  |  |  |  |



Figure 13 - Statement of Question 2 of the Middle School (3 ${ }^{\text {rd }}$ level).

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Source: D-Estat data.
In Figure 14, we see that students performed worse in calculating the means per line (adding and dividing by two) and tests (dividing by 5). Less than half managed to add the columns. The failure in the overall mean made it difficult to make comparisons. We also observed that few students realized that increasing the score in the $2^{\text {nd }}$ test by two points would increase the mean in the $2^{\text {nd }}$ test by two points, and that this would impact one point in the overall mean, since there were two score. Few students were successful in this task.


Figure 14 - Percentage of correct answers for Middle School students in Question 2, per school grade. Source: D-Estat data.

When we elaborated the question, we believed that students would be very familiar with calculating the mean of the scores in tabular representation. In Figure 15 we present the extracts from the resolution of two students, in which we observe that the students perform the additions by lines (scores of each student) and columns (scores in each test) correctly, but the one on the left apparently added the three columns and divided it by three, which could be an indication of the mean concept, but which still needs instruction. The student on the right joined the two numbers, considering the score in the first test as the integer and the score in the second test as part of the decimal, signaling that he has no idea of the mean concept.

| Figure 1 - Score of 5 students in both tests $1^{\text {st }}$ test, $2^{\text {nd }}$ test, Total of both tests, Mean <br> Quadro 1 - Nota de cinco estudantes nas duas provas |  |  |  |  | Figure 1 - Score of 5 students in both tests $1^{\text {st }}$ test, $2^{\text {nd }}$ test, Total of both tests, Mean <br> Quadro 1 - Nota de cinco estudantes nas duas provas |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1^{1}$ prova | $2^{\text {a }}$ prova | Total nas duas provas | Média |  | $1^{\text {a }}$ prova | $2^{\text {a }}$ prova | Total nas duas provas | Média |
| Bia | 7 | 3 | 10 |  | Bia | 7 | 3 | 10 | 7,3 |
| Luiz | 7 | 3 | 10 | , | Luiz | 7 | 3 | 10 | 7.3 |
| Cléo | 8 | 4 | 12 | 8 | Cléo | 8 | 4 | 12 | 8,4 |
| Nina | 6 | 24 |  | 6 | Nina | 6 | 2 | 8 | 6,2 |
| Joăo | 7 | 3 | 10 |  | João | 7 | 3 | 10 | 7,3 |
| Total de pontos do grupo | 35 | 15 |  |  | Total de pontos do grupo | 35 | 15 |  |  |
| Total scores of both groups |  |  |  |  | Total scor | of both g | oups |  |  |

Figure 15 - Solution of two $9^{\text {th }}$ grade students in determining the average per line.
Source: D-Estat data.
The drop in performance, when compared to Question 1, appears to indicate that students are not familiar with data in tabular registries. We observed that Luna and Carvalho (2019) found that the presentation of data in graphs hindered student performance. In the present study it seems that students are not used to working with data in tabular representation.

Question 3 was similar to that of the early years, but in a TDF double entry (Figure 16). It requested 10 more complex tasks, as it required an advanced level of data reading: the sum per line (Tot-line); the sum of the columns (Tot-C1, Tot-C2 and Tot-C3); the relative frequency of dogs for girls ( $\% \mathrm{~F}$ ); for boys ( $\% \mathrm{M}$ ), establish a relationship between these relative frequencies (Relat1); indicate the relationship (Which1), the perception of the relationship between the variables (Relat2) and indicate the type of relationship (Which2).

| Figure 2 - Number of students by gender, according to favorite pet |  |  |  | Q3a. Fill in the Figure 2 with the total with which each animal was chosen. <br> Q3b. How many boys responded to the survey? How many girls? In all, how many students responded to the survey? |
| :---: | :---: | :---: | :---: | :---: |
| Favorite pet | Gender |  | Total |  |
|  | Boys | Girls |  |  |
| Cat | 0 | 75 |  | Q3c. Percentage of girls that chose Dog? |
| Bird | 15 | 15 |  | Q3d. Percentage of boys that chose Dog? |
| Dog | 25 | 50 |  | Q3e. Analyzing the data in the Figure 2 and the |
| Others (monkey, tortoise, etc.) | 5 | 5 |  | calculated percentages, can we say that girls prefer dogs more than boys? () No () Yes. Why? |
| None | 5 | 5 |  | Q3f. Analyzing the data in the Figure 2, in your |
| Total students |  |  |  | opinion, is there evidence of a relationship between the favorite pet and being a boy or girl? () No () Yes. |

Figure 16 - Statement of Question 3 of the Middle School.
Source: D-Estat data.
Figure 17 shows that the sum by lines was better performed than the sum by columns, and this execution was better performed according to the students' school grade. Very few students were able to calculate the relative frequency, the majority repeated the absolute frequency plus the symbol $\%$, and the concept of percentage has been in the curriculum since the $5^{\text {th }}$ grade. Few students were able to see the relationship between the variables, and when they made that relationship explicit, the justifications were given from their beliefs and not from the data.

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Figure 17 - Percentage of correct answers for Middle School students in Question 3, per school grade.
Source: D-Estat data.
Finishing the analysis of student performance in the final years, we present Figure 18.


Figure 18 - Percentage distribution of correctness, error and blank, by item, of students of the Middle School. Source: D-Estat data.

We observed that the percentage of correct answers drops significantly in relation to the two other levels, and the percentage of blank answers increases considerably. The items that presented the highest percentage of blank responses, greater than $50 \%$, were those that requested the name of the statistical concept, mean, median and identifying the relationship between gender and favorite pet. We believe that these were also the items expected to cause the majority of incorrect answers, as school activities usually do not address the name of the concepts and do not require more than the elementary level of interpretation of a table or graph.

## Global analysis of the performance of elementary school students

In this section, we draw parallels regarding performance in the three School levels. In Question 1 we can see that, in general, there is a performance increase over the school grade within each level, but there is a drop from one level to another, especially in the Middle School, particularly in the $9^{\text {th }}$ grade.

In the conversion of native language data ( $1^{\text {st }}$ level) and list ( $3^{\text {rd }}$ level) to graphic representation (G.Bars), we see a clear performance increase in the Elementary School, going from less than $30 \%$, in the $1^{\text {st }}$ grade, to little more than $80 \%$ in the $5^{\text {th }}$ grade; however, we observed stagnation in the final grade, at the level of $60 \%$, with the exception of the $8^{\text {th }}$ grade students, which reaches about $75 \%$, but still below the performance achieved by the $5^{\text {th }}$ grade students.

Among the main mistakes made in the conversion of native language data to the students' graphic registry, we exhibit them in Figure 19.


Figure 19 - Examples of errors when converting data to the bar graph.
Source: D-Estat data.
We found that in the Elementary School, some students who drew the correct quantity of rectangles, drew some bars without starting at the zero scale (19a), showing that they are still unable to relate the ordinate axis to the number of rectangles in each bar. Others drew the bars together (19b), in the order in which the data appeared, but were unable to relate the name of each child to the column; in the final years some students tried to make a line graph
(19c) and built a "band" graph (19d), and other depictions. These results lead us to agree with the conclusions of Carvalho, Oliveira and Monteiro (2019) regarding the need for teachers to emphasize the systematization of statistical information and the use of scale in bar graphs.

With regard to Mode, more than $60 \%$ of students in the $1^{\text {st }}$ level were able to identify the amount that was repeated the most, in the Middle School this was not achieved in the 9th grade, which instead of answering that the amount spent most often was R $\$ 4.00$, answered the maximum amount of expenses, $\mathrm{R} \$ 10.00$. Similarly, in the $5^{\text {th }}$ grade, instead of answering that the number of marbles that were more repeated was 4 , they answered the maximum amount, which was 10 marbles. These results are inconsistent with what is expected to occur: that the higher level of education leads to greater performance, as in the study by Luna and Carvalho (2019).

As for addition (Figure 20), we found that the performance of the $1^{\text {st }}$ to the $3^{\text {rd }}$ grade students went from $40 \%$ to $60 \%$, with many students using pictorial representation as shown in Figure 20a; the performance of students in the $4^{\text {th }}$ and $5^{\text {th }}$ grades was around $50 \%$, and those in the Middle School went from $60 \%$ in the $6^{\text {th }}$ grade, to $80 \%$ in the $8^{\text {th }}$ and $9^{\text {th }}$ grades. Many students recorded several types of grouping, most of whom performed the correct calculation (20d). In Figure 20b and 20c we illustrate the calculation error.

| (a) $1^{\text {st }}$ grade, correct answer Q1.c In all, how many marbles do the 5 children have? <br> Q1c. Ao todo, quantas bolas de gude têm as cinco crianças? |  |  |  |  |  |  | (b) $5^{\text {th }}$ grade, incorrect answer <br> Q1.b In all, how many marbles do the 7 children have? <br> Q1b. Ao todo, quantas bolas de gude têm as sete crianças |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | - $2+9+4+5=5$ |
| (b) 8th grade, incorrect answer |  |  |  |  |  |  | (d) $5^{\text {th }}$ grade, correct answer <br> Q1b. Ao todo, quantas bolas de gude têm as sete cria |
| Segunda | Terca | Quarta | Quinta | Sexta | Sábado | Doming | $4+6+4+50+9+45=$ |
| $\text { R } \$ 4,00$ | $\text { R\$ } 4,00$ | $R \$ 4,00$ | $\text { R\$ } 5,00$ | $\text { R } \$ 6,00$ | $\text { R\$ } 10,00$ | RS 9,00 | $\begin{gathered} 34+10+9+4+5= \\ 24+9+4+5 \\ 33+4+5 \\ 325 \end{gathered}$ |

Figure 20 - Registry of the sum of some students.
Source: D-Estat data.
Regarding the mean, there is a substantial performance drop from one level to another, in which the numbers involved were small and the division exact, which allowed the use of alternative strategies for the division algorithm, as shown in Figure 21.

We observed that, in general, the rate of correct answers in the $1^{\text {st }}$ level was $10 \%$ in the $1^{\text {st }}$ grade to $45 \%$ in the $3^{\text {rd }}$ grade; in the $4^{\text {th }}$ grade it was around $25 \%$ and in the $5^{\text {th }}$ grade $30 \%$. In the Middle School, this index increased from $5 \%$ in the $6^{\text {th }}$ grade to $30 \%$ in the $8^{\text {th }}$ grade and dropped to $20 \%$ in the $9^{\text {th }}$ grade.

Figure 21a shows that $3^{\text {rd }}$ grade students used different types of pictorial representations; the $4^{\text {th }}$ and $5^{\text {th }}$ grade students used a mixture of the division algorithm and
representation with drawings (Figure 21b) and, in general, the students of the final grade only recorded the final result and most of them were wrong. In Figure 21c we illustrate the difficulty of an $8^{\text {th }}$ grade student in the division algorithm, compromising the calculation of the mean, as in the results found by Luna and Carvalho (2019).

Regarding the performance in Question 2, whose data were presented in tabular register, we observed that, in the 1st level, after stagnation in the first two years, there is a significant increase in the $3^{\text {rd }}$ grade; a substantial drop in the $4^{\text {th }}$ and $5^{\text {th }}$ grades and an even greater drop in the final grades.


Figure 21 - Records of the mean of some students.
Source: D-Estat data.
Observing that in the $1^{\text {st }}$ level it was a statistical table, with four numbers, the sum of which was 12 , the $3^{\text {rd }}$ grade students did relatively well in the sum and mean, often using the division in equal parts and pictorial representation, as shown Figure 22.


Figure 22- Register of the mean calculation of a $3{ }^{\text {rd }}$ grade student.
Source: D-Estat data.
With regard to the median, we can see that some students ordered the numbers correctly (Figure 23), but practically none could perceive that the median was between the
two values that occupied the central positions. This result is in agreement with the results of Mayén et al. (2007) who found that Mexican and Spanish students also found it difficult to determine the median due to the indeterminacy produced by having two central values. In addition, stating that the median is 16 shows that the student does not know that the median can only take values between the minimum and maximum values.

| $1^{\text {st }}$ position $-2^{\text {nd }}$ position $-3^{\text {rd }}$ position $-4^{\text {th }}$ position |  |  |  |
| :---: | :---: | :---: | :---: |
| $1^{\text {a }}$ posição | $2^{\text {a }}$ posição | $3^{\text {a }}$ posição | $4^{\text {a }}$ posição |
| 0 | 8 | 9 | 11 |
| What is the number of chocolate snacks that occupies the central position? <br> Q2d. Qual é a quantidade de brigadeiros que ocupa a posição central? |  |  |  |
| 16 aue e Daminajo. |  |  |  |

Figure 23 - Ordination and attempt to determine the median by a $5^{\text {th }}$ grade student.
Source: D-Estat data.
Regarding Question 3, we found that in the Mode extraction (identifying the maximum in frequency distribution table), the $4^{\text {th }}$ grade students have the worst performance and the $5^{\text {th }}$ grade students tie with the $3^{\text {rd }}$ grade students. This is worrying, as according to Curcio (1989) it is an elementary level reading. As for the sum, we observe that there are six numbers that change only the order of magnitude, therefore the drop in the $4^{\text {th }}$ and $5^{\text {th }}$ grade students is not justified. Similarly, the performance of the Middle School is worrying.

## Final Considerations

The results of the present investigation are quite worrying, considering that the contents of Statistics in Elementary Education were inserted in 1997, but most students do not know how to identify the nomenclature when determining mean, median and mode. The results indicate that students are not familiar with the presentation of data in tabular or graphical register, corroborating the results of recent studies (Luna \& Carvalho, 2019; Carvalho, Oliveira \& Monteiro, 2019).

The level of tables and graphs-reading by students is nothing more than elementary, according to the classification of Curcio (1989) and Wainer (2002). The student that confused the mean with the most frequent value (Mode), with the maximum value or with the sum, has also been reported in other studies (Cobo \& Batanero, 2004 and Mayén et al., 2007).

The results show that students have limitations with fundamental operations (addition and division) and reading comprehension, which are components of statistical literacy (Gal, 2002).

As study limitations, we inform that in recent years, our partner schools have been suffering from the lack and changes of mathematics teachers, strikes and interruptions. We also noticed that many students, especially from the Middle School, left questions unanswered (blank). However, this survey was also carried out in schools in Ceará, Natal and

São Paulo, which will allow verifying the local effect. In addition, we have been working with teachers at these schools for almost two years and a new survey is expected in 2020, when we expect more promising results.

Finally, we reiterate the need to develop teaching sequences that address topics of interest to students, as proposed by Santana (2006), which allow the use of different types of representation and registers such as those presented by Nascimento, Paula and Carneiro (2018) to contribute to the learning of statistical concepts, to mediate conflicts, to make personal or collective decisions as highlighted by Teixeira (2006), and to develop an inquisitive stance, making use of critical thinking as postulated by Gal (2002), Skovsmose (2008) and Santos and Branches (2019).

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